## **CENTRIPETAL ACCELERATION**

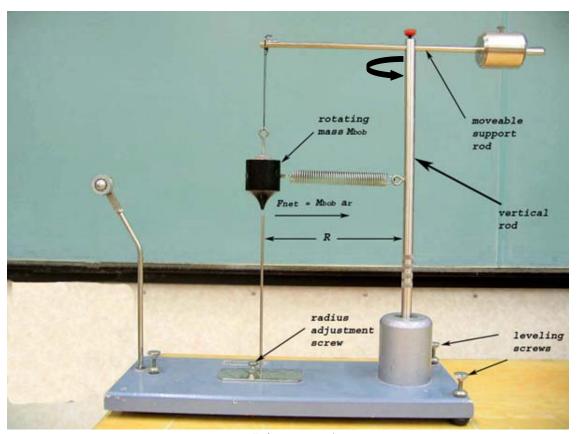
# **OBJECTIVE**

To calculate the net force on an object moving in uniform circular motion and compare with the expected value.

# **THEORY**

### A. Mass Rotating in Uniform Circular Motion

Consider the *Centripetal Force Apparatus* below. The mass  $M_{bob}$  is rotating in uniform circular motion about the vertical rod in a radius R.



# Diagram 1

Applying Newton's  $2^{\rm nd}$  Law in the radial direction gives a net force in the radial direction given by  $F_{\rm net} = M_{\rm bob} a_r$  where  $a_r = \frac{v^2}{R}$ . The speed of the mass  $M_{\rm bob}$  is given by  $v = \frac{2\pi R}{T}$  and thus  $a_r = \frac{4\pi^2 R}{T^2}$ . Therefore,  $F_{\rm net} = M_{\rm bob} \frac{4\pi^2 R}{T^2}$ .

#### B. Mass in Equilibrium

Now let's consider the case when the mass  $M_{bob}$  is in equilibrium and the radius R is the same as it was when it was rotating in uniform circular motion. If this is the case, then the tension force which equals the weight of the hanging mass  $W_{hanging}$ , must be equal to the net force in the radial direction  $F_{net} = M_{bob} \frac{4\pi^2 R}{T^2}$  when the mass  $M_{bob}$  was rotating in uniform circular motion. We will be comparing these two values taking  $W_{hanging}$  to be the expected value.

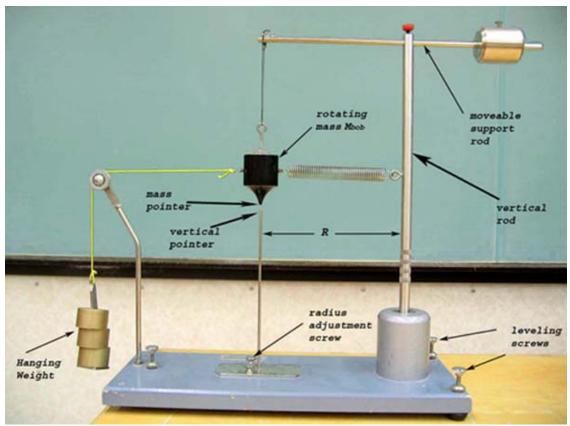


Diagram 2

# **EQUIPMENT**

- 1. centripetal force apparatus
- 2. set of masses and hanger
- 3. stopwatch
- 4. string
- 5. level
- 6. ruler

## **PROCEDURE**

### <u>Part 1(Uniform Circular Motion – see Diagram 1)</u>

- 1. Remove mass  $M_{bob}$  from apparatus and measure the mass with triple-beam balance. Place mass  $M_{bob}$  back on the apparatus but do not attach spring
- 2. With the spring not attached, level the platform with the level and align the mass pointer with the vertical pointer.
- 3. Measure the radius R.
- 4. Attach spring to mass M<sub>bob</sub>.
- 5. Rotate M<sub>bob</sub> at constant speed so that bob pointer is aligned with the vertical pointer.
- 6. Measure the time for 20 revs 3 times and calculate the average period.
- 7. Calculate the radial acceleration a<sub>r</sub> using the average period.
- 8. Calculate the net force  $F_{net}$  in the radial direction.

#### Part 2 (Static Equilibrium – see diagram 2)

- 1. Leave the spring attached to mass M<sub>bob</sub>.
- 2. Attach string with hanger to mass M<sub>bob</sub>.
- 3. Add mass to hanger until the mass pointer and vertical pointer are aligned just as it was when  $M_{bob}$  was rotating in uniform circular motion.
- 4. Calculate weight W<sub>hanging</sub> of hanging mass.
- 5. Compare  $W_{hanging}$  with  $F_{net}$ . Take  $W_{hanging}$  to be the accepted value and use  $g = 9.80 \text{ m/s}^2$ .
- 6. Repeat Part (1) and Part (2) above for a total of 4 different radii.

Construct a data table like the following in your lab report:

R (cm)	M <sub>bob</sub> (kg)	t <sub>1</sub> (20 revs)	$T_1(s)$	t <sub>2</sub> (20 revs)	$T_2(s)$	$t_3(20 \text{ revs})$	$T_3(s)$	Tave

R (cm)	$a_{r}$	$F_r(N)$	M <sub>hanging</sub> (kg)	$W_{hanging}(N)$	%error